

Notes 6.3

The point (x, y) relates to (cos θ , sin θ)

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad (\theta = \text{angle measure})$$

For problems 1 - 3, determine the exact values of all six trigonometric functions of the given angle.

1. $\frac{5\pi}{4}$

$$\sin \frac{5\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\cos \frac{5\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\tan \frac{5\pi}{4} = 1$$

$$\csc \frac{5\pi}{4} = -\sqrt{2}$$

$$\sec \frac{5\pi}{4} = -\sqrt{2}$$

$$\cot \frac{5\pi}{4} = 1$$

2. $\frac{5\pi}{6}$

$$\sin \frac{5\pi}{6} = \frac{1}{2}$$

$$\cos \frac{5\pi}{6} = -\frac{\sqrt{3}}{2}$$

$$\tan \frac{5\pi}{6} = -\frac{\sqrt{3}}{3}$$

$$\csc \frac{5\pi}{6} = 2$$

$$\sec \frac{5\pi}{6} = -\frac{2\sqrt{3}}{3}$$

$$\cot \frac{5\pi}{6} = -\sqrt{3}$$

3. $\frac{-1\pi}{2}$

$$\sin \frac{-1\pi}{2} = -1$$

$$\cos \frac{-1\pi}{2} = 0$$

$$\tan \frac{-1\pi}{2} = \text{undefined}$$

$$\csc \frac{-1\pi}{2} = -1$$

$$\sec \frac{-1\pi}{2} = \text{undefined}$$

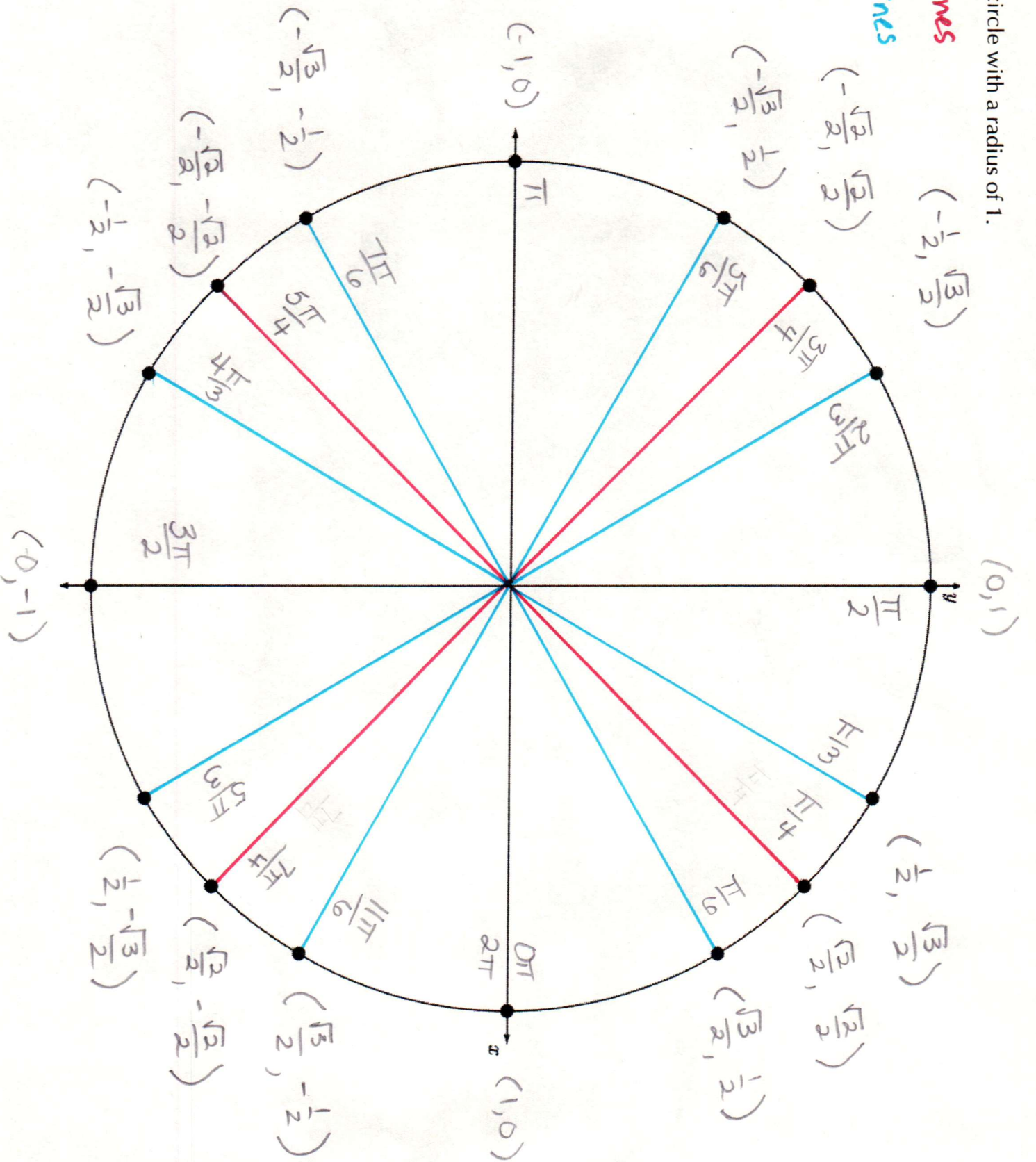
$$\cot \frac{-1\pi}{2} = 0$$

$$-\frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\sqrt{2}$$

A circle with a radius of 1.

$\frac{1}{4}\pi$ lines

$\frac{1}{6}\pi$ lines



When converting between degrees and radians you set up a proportion. You can use either of these set-ups.

$$\frac{\text{degrees}}{360^\circ} = \frac{\text{radians}}{2\pi}$$

$$\text{or } \frac{\text{degrees}}{180^\circ} = \frac{\text{radians}}{\pi}$$

Convert the angles from degrees to radians. Write exact answers.

$$4. \quad 100^\circ \quad \frac{100^\circ}{360^\circ} = \frac{x}{2\pi} \quad 200\pi = 360x \quad \frac{200\pi}{360} = x \quad \boxed{x = \frac{5\pi}{9}}$$

$$5. \quad -76^\circ \quad \frac{-76}{180^\circ} = \frac{x}{\pi} \quad -76\pi = 180x \quad \frac{-76\pi}{180} = x \quad \boxed{x = \frac{-19\pi}{45}}$$

$$6. \quad 155^\circ \quad \frac{155}{180} = \frac{x}{\pi} \quad 155\pi = 180x \quad \frac{155\pi}{180} = x \quad \boxed{x = \frac{31\pi}{36}}$$

Convert the angles from radians to degrees. Write exact answers.

$$7. \quad \frac{4\pi}{7} \quad \frac{x}{180} = \frac{\frac{4\pi}{7}}{\pi} \quad x\pi = \frac{720}{7}\pi \quad \boxed{x = \frac{720}{7}^\circ} \approx 102.86^\circ$$

$$8. \quad \frac{-5\pi}{2} \quad \frac{x}{180} = \frac{\frac{-5\pi}{2}}{\pi} \quad x\pi = -450\pi \quad \boxed{x = -450^\circ \text{ or } -90^\circ}$$

$$9. \quad \frac{13\pi}{8} \quad \frac{x}{180} = \frac{\frac{13\pi}{8}}{\pi} \quad x\pi = \frac{585}{2}\pi \quad \boxed{x = \frac{585}{2}^\circ \text{ or } 292.5^\circ}$$

$$10. \quad 480^\circ \text{ is the same as } \underline{120^\circ} :.$$

$$480 - 360 =$$